March 8, 2016

## Practice Exam 2

No calculators. Show your work. Clearly mark each answer.

1. (20 points) Find the general solution for the system

$$y'' + 6y' + 5y = e^t$$

Solve with initial conditions y(0) = 0, y'(0) = 1.

2. (20 points) Find the general solution for the problem

$$\frac{dx}{dt} = x$$
$$\frac{dy}{dt} = x + 2y.$$

Solve with initial conditions x(0) = 0, y(0) = 1.

3. (20 points) The following system describe a pair of competing species. Describe the long-time likely outcome of the competition by plotting the direction field.

$$\frac{dx}{dt} = x(2 - x - y)$$
$$\frac{dy}{dt} = y(3 - x - y).$$

Draw the curves x(t) and y(t) if x(0) = 1, y(0) = 1 and x(0) = 10, y(0) = 1 in the phase plane.

4. (20 points) The following system describe a pair of competing species. Describe the long-time likely outcome of the competition by plotting the direction field.

$$\frac{dx}{dt} = x(2 - x - y)$$
$$\frac{dy}{dt} = y(3 - x - 3y).$$

Draw the curves x(t) and y(t) if x(0) = 5 and y(0) = 2 in the phase plane.

5. (20 points) Compute the Euler's approximate solution at time t = 1 of the following system

$$\frac{dx}{dt} = x(2 - x - y)$$
$$\frac{dy}{dt} = y(1 - x - y).$$

With initial position x(0) = 1 and y(0) = 1 and time step  $\Delta t = 0.5$