

Math 104Q
University of Connecticut

Group Project on Linear Equations: How Many Bees in Lilavati's Swarm?

In twelve century AD there lived in India a famous mathematician by the name Bhaskara. His contributions to mathematics were so remarkable that a medieval inscription in an Indian temple reads:

“Triumphant is the illustrious Bhaskara whose feats are revered by both the wise and the learned. A poet endowed with fame and religious merit, he is like the crest on a peacock.”

And indeed, as it was the custom in India of his days, all of Bhaskara's mathematical works were written in verse. His most charming book, *Lilavati*, written for his daughter, whose nickname was Lilavati (The beautiful), contains many interesting algebraic poems. Apparently beautiful Lilavati, following in her father's footsteps, had a taste for higher mathematics.

Here is one poem from *Lilavati*:

*A fifth part of a swarm of bees came to rest
on the flower of Kadamba,
a third on the flower of Silinda.
Three times the difference between these two numbers
flew over a flower of Krutaja,
and one bee alone remained in the air,
attracted by the perfume of a jasmine in bloom.
Tell me, beautiful girl, how many bees were in the swarm?*

Follow the four steps followed by Lilavati to find the answer to the question posed in the poem:

1. UNDERSTAND the problem thoroughly.

Read: Read and reread the poem.

Trial and Error: Check if a few arbitrary values give you a solution. For example, check if a swarm of 6 bees satisfies all the conditions of the poem. Pick your own additional values for the number of bees in the swarm, and try them out. Reflect on your answers. After three or more trials make a guess of what the solution will be?

2. TRANSLATE the problem into an equation.

Chose a variable to represent the unknown: Let $x =$

Write an equation in x for your problem:

3. SOLVE the equation for x .

4. INTERPRET.

Check your solution:

State your answer:

Preparation for Sciences: Integrating Intermediate Algebra and Mathematical Modeling
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Solution to: How Many Bees in Lilavati's Swarm?

Set x = the number of bees in the swarm.

We have:	• over the flower of Kadamba:	$\frac{x}{5}$
	• over the flower of Silinda:	$\frac{x}{3}$
	• over the flower of Krutaja:	$3\left(\frac{x}{3} - \frac{x}{5}\right)$
	• in the air:	1
		<hr/>
TOTAL:		$\frac{x}{5} + \frac{x}{3} + 3\left(\frac{x}{3} - \frac{x}{5}\right) + 1$

The equation becomes:

$$\frac{x}{5} + \frac{x}{3} + 3\left(\frac{x}{3} - \frac{x}{5}\right) + 1 = x$$

To solve it we first eliminate parenthesis:

$$\frac{x}{5} + \frac{x}{3} + 3\frac{x}{3} - 3\frac{x}{5} + 1 = x$$

LCD = 15

Multiply both sides of the equation by 15:

$$15 \cdot \frac{x}{5} + 15 \cdot \frac{x}{3} + 15 \cdot 3\frac{x}{3} - 15 \cdot 3\frac{x}{5} + 15 \cdot 1 = 15 \cdot x$$

Reduce all fractions (to get rid of denominators):

$$3x + 5x + 15x - 9x + 15 = 15x$$

Combine like terms:

$$14x + 15 = 15x$$

Subtract 14x on both sides:

$$15 = 15x - 14x$$

Solution:

$$x = 15$$

Answer: There are 15 bees in Lilavati's swarm.