Math 5020: Introduction to Commutative Algebra Sarah Glaz

Assignment #1

A. Exercises from your textbook (Atiyah & MacDonald: Intro to Commutative Algebra):

Pages 10-16: exercises 1, 2, 7, 11, 12, 15, 16

- **B.** Let *A* be a commutative ring. Show that *A* is a field iff every ideal of *A* is prime.
- **C.** A commutative ring *A* is called Von Neumann regular (abbreviated VNR) is for every element $a \varepsilon A$ there is an element $b \varepsilon A$ such that $a^2b = a$. Show that A is VNR iff every ideal *I* of *A* is a radical ideal (that is, *I* is equal its own radical). [Hint: use Exercise 1.13 (iii) on page 9 of your textbook].