

MATH 3630 - Actuarial Mathematics I  
Fall 2008 - Valdez  
Homework No. 4  
due Wednesday, 6:50 PM, October 22, 2008

Please return this page with your signature. Please write your name and student number at the spaces provided:

Name: SUGGESTED SOLUTION Student ID: EMIL

I certify that this is my own work, and that I have not copied the work of another student.

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A life insurance policy is issued to age 30 with the following decreasing scale of death benefits:

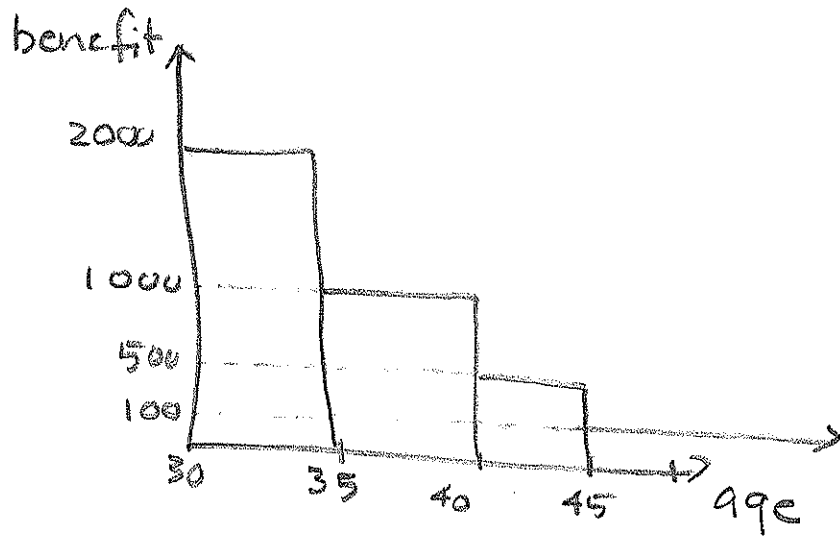
age	death benefit
30-35	2,000
35-40	1,000
40-45	500
over 45	100

Assume the benefits are payable at the end of the year of death and that:

- mortality follows the Illustrative Life Table; and
- $i = 6\%$ .

Calculate the actuarial present value of the benefits for this policy. (Your answer must be a number!)

# Homework 4



$$\begin{aligned}
 APV &= 2000 A_{30:\overline{5}|} \\
 &+ 1000 {}_5E_{30} A_{35:\overline{5}|} \\
 &+ 500 {}_{10}E_{30} A_{40:\overline{5}|} \\
 &+ 100 {}_{10}E_{30} {}_5E_{40} A_{45}
 \end{aligned}$$

where

$$\begin{aligned}
 A_{30:\overline{5}|} &= A_{30} - {}_5E_{30} A_{35} = \frac{102.48}{1000} - \frac{740.91}{1000} \frac{128.72}{1000} \\
 &= 0.007110
 \end{aligned}$$

$$\begin{aligned}
 A_{35:\overline{5}|} &= A_{35} - {}_5E_{35} A_{40} = \frac{128.72}{1000} - \frac{738.73}{1000} \frac{161.32}{1000} \\
 &= 0.009548
 \end{aligned}$$

$$\begin{aligned}
 A_{40:\overline{5}|} &= A_{40} - {}_5E_{40} A_{45} = \frac{161.32}{1000} - \frac{735.29}{1000} \frac{201.20}{1000} \\
 &= 0.013380
 \end{aligned}$$

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The APV of the benefits equals

$$\text{APV} = 2000(.00711) + 1000(.74091)(.009548) \\ + 500(.54733)(.013380) + 100(.54733)(.73529)(.20120)$$

$$= 14.22013 + 7.074265 + 3.661542 + 8.097219$$

$$= \underline{\underline{33.05316}}$$