

MATH 3630 - Actuarial Mathematics I
 Fall 2011 - Valdez
 Homework No. 3
 due Wednesday, 5:00 PM, 19 October 2011

Please return this page with your signature. Please write your name and student number at the spaces provided:

Name: SUGGESTED SOLUTIONS Student ID: _____

I certify that this is my own work, and that I have not copied the work of another student.

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You are given that for a whole life insurance issued to (x) that pays \$100 at the moment of death:

- The actuarial present value of the policy is \$60.00 based on a constant force of mortality μ and a constant force of interest equal to 0.02. $\Rightarrow 100 \left(\frac{\mu}{\mu+0.02} \right) = 60$
- The actuarial present value of the policy is \$63.64 based on a constant force of mortality $\mu + c$ and a constant force of interest equal to 0.02. $\Rightarrow 100 \left(\frac{\mu+c}{\mu+c+0.02} \right) = 63.64$

1. Determine the values of μ and c .
2. Calculate the actuarial present value of the policy based on a constant force of mortality μ and a constant force of interest $0.02 + c$, where μ and c are the constants determined in 1.
3. Calculate the actuarial present value of the policy based on the force of mortality

$$\mu_{x+t} = \begin{cases} \mu, & \text{for } 0 < t \leq 15 \\ \mu + c, & \text{for } t > 15 \end{cases}$$

and the force of interest

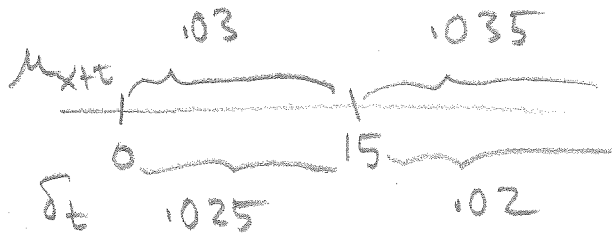
$$\delta_t = \begin{cases} 0.02 + c, & 0 < t \leq 15 \\ 0.02, & \text{for } t > 15 \end{cases}$$

where μ and c are the constants determined in 1.

$$\begin{aligned} \textcircled{1} \quad \frac{\mu}{\mu+0.02} &= \frac{60}{100} = .6 \Rightarrow \mu = .6\mu + 0.12 \Rightarrow \mu = \frac{0.12}{.4} = .03 \\ \frac{\mu+c}{\mu+c+0.02} &= \frac{63.64}{100} = .6364 \Rightarrow \frac{0.03+c}{0.05+c} = .6364 \Rightarrow c = \frac{.6364(0.05) - .03}{1 - .6364} \\ &= .005 \end{aligned}$$

$$\textcircled{2} \quad APV(\text{policy}) = \frac{100 \mu}{\mu + 0.02 + C} = 100 \frac{0.03}{0.03 + 0.02 + 0.005} = \underline{\underline{54.54}}$$

$$\textcircled{3} \quad \mu = 0.03, \quad \mu + C = 0.035, \quad C = 0.005$$



$$APV(\text{policy}) = 100 \left[\frac{0.03}{0.055} (1 - e^{-0.055(15)}) + e^{-0.055(15)} \cdot \frac{0.035}{0.055} \right]$$

$$= \underline{\underline{58.53}}$$