

**MATH 3630 - Actuarial Mathematics I**  
**Fall 2010 - Valdez**  
**Homework No. 3**  
**due Wednesday, 6:15 PM, 20 October 2010**

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For a special whole life insurance on  $(x)$  payable at the moment of death, you are given:

- Mortality of  $(x)$  follows de Moivre's law.
- The probability that  $(x)$  survives another 24 years is 0.70.
- The force of interest is expressed as

$$\delta_s = \begin{cases} 0.05, & \text{for } 0 < s \leq 20 \\ 0.10, & \text{for } s > 20 \end{cases}$$

- The death benefit at time  $t$  is  $b_t = 100(1.05)^t$ , for  $t > 0$ .
- The present value random variable for this insurance at issue is denoted by  $Z$ .

1. (5 points) Calculate the Actuarial Present Value (APV) of the benefit for this insurance.
2. (5 points) Calculate the variance of  $Z$ .