MATH 3630<br>Actuarial Mathematics I<br>Class Test 1 - 3:35-4:50 PM<br>Wednesday, 27 September 2017<br>Time Allowed: 1 hour<br>Total Marks: 100 points

Please write your name and student number at the spaces provided:

Name: $\qquad$ Student ID:

- There are ten (10) written-answer questions here and you are to answer all ten. Each question is worth 10 points.
- Please provide details of your workings in the appropriate spaces provided; partial points will be granted.
- Please write legibly.
- Anyone caught writing after time has expired will be given a mark of zero.

Question No. 1:
In a population today, all of equal age $x$, consisting of $25 \%$ non-smokers and $75 \%$ smokers, you are given:

- Mortality for non-smokers follows a constant force of mortality of 0.01 .
- Mortality for smokers follows a constant force of mortality of $0.01 h$, for some positive $h$.
- In 55 years, there will exactly be equal proportions of non-smokers and smokers.

Calculate $h$.

Question No. 2:
You are given:

- ${ }_{5} p_{x}=0.96$
- ${ }_{8} p_{x}=0.90$

Calculate ${ }_{3} q_{x+5}$.

## Question No. 3:

You are given the following survival function of a newborn:

$$
S_{0}(x)=\exp \left[-(2 x / 15)^{3 / 4}\right], \quad \text { for } x \geq 0
$$

Calculate the force of mortality at age $45, \mu_{45}$.

Question No. 4:
For a life $(x)$, you are given the following extract from a life table:

| $k$ | $\ell_{x+k}$ |
| :--- | ---: |
| 0 | 10,000 |
| 1 | 9,875 |
| 2 | 9,625 |
| 3 | 9,275 |
| 4 | 8,775 |
| 5 | 8,025 |

Calculate ${ }_{3 \mid 2} q_{x}$ and interpret this probability.

## Question No. 5:

You are given:

- Mortality follows De Moivre's law with parameter $\omega$.
- $\dot{e}_{20: \overline{20}}=18$

Calculate ${ }_{30 \mid 10} q_{30}$.

## Question No. 6:

Suppose you are given the following extract from a life table:

| $x$ | $\ell_{x}$ |
| ---: | ---: |
| 94 | 15,000 |
| 95 | 12,500 |
| 96 | 8,750 |
| 97 | 4,375 |
| 98 | 1,530 |
| 99 | 380 |
| 100 | 40 |
| 101 | 0 |

Calculate $e_{95}$.

## Question No. 7:

You are given:

- The probability that (35) survives to reach age 50 is 0.83 .
- The probability that (35) dies between the ages of 50 and 65 is 0.15 .
- $\ell_{65}=6800$

Calculate $\ell_{35}$.

## Question No. 8:

Mortality follows the Generalized De Moivre's law expressed as:

$$
S_{0}(x)=\left(1-\frac{x}{100}\right)^{1 / 2}, \text { for } 0 \leq x \leq 100
$$

Calculate the probability that life (35) will die between ages 50 and 65.

## Question No. 9:

The force of mortality for a substandard life $(x)$ is expressed as

$$
\mu_{x+t}^{s}=\mu_{x+t}+a,
$$

for some constant $a>0$, where $\mu_{x+t}$ is the force of mortality of a standard life $(x)$. You are given:

- The probability that a standard life $(x)$ survives the next 10 years is 0.70 .
- The probability that a substandard life $(x)$ survives the next 10 years is 0.63 .

Calculate the value of the constant $a$.

Question No. 10:
Please complete the rest of the life table below:

| $x$ | $\ell_{x}$ | $d_{x}$ | $p_{x}$ | $q_{x}$ |
| :---: | :---: | :---: | :---: | :---: |
| 96 | 100 |  |  |  |
| 97 | 85 |  |  |  |
| 98 | 65 |  |  |  |
| 99 | 35 |  |  |  |
| 100 | 0 |  |  | na |

na $=$ not applicable

EXTRA PAGE FOR ADDITIONAL OR SCRATCH WORK

