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Score: \_\_\_\_\_\_/20

## Classifying Critical Points

Please staple your work and use this page as a cover page.

- 1. Find and classify all critical points of the function  $f(x,y) = x^3 6xy y^2$
- 2. Find and classify all critical points of the function  $f(x,y) = 5xye^{-y^2}$ .
- 3. Show that the function  $f(x,y) = x^2 + 4y^2 4xy + 2$  has an infinite number of critical points and that D = 0 at each one.
- 4. For a function of one variable, it is impossible for a continuous function to have, for example, two local maxima without a local minimum (or vice versa). However, for functions of two or more variables, such functions exist. Given the function

$$f(x,y) = -(x^2 - 1)^2 - (x^2y - x - 1)^2,$$

show that (-1,0,0) and (1,2,0) are critical points and that both are local maxima. (In fact, these two points are the only critical points for this function).